

Prof. Dr. Alfred Toth

Trajektionen semiotischer Differentiation

1. Zwei mal vier bifunktorielle Produkte (vgl. Toth 2025a, b)

$(a.b), (c.d) =$

1. $(a.c), (b.d)$ | 2. $(d.b), (c.a)$

3. $(b.c), (a.d)$ | 4. $(d.a), (c.b)$

5. $(a.d), (b.c)$ | 6. $(c.b), (d.a)$

7. $(b.d), (a.c)$ | 8. $(c.a), (d.b)$

2. Im folgenden zeigen wir die obigen 8 Möglichkeiten, semiotische Dyadenpaare abzuleiten und bestimmen die zugehörigen Trajektionen. Sei

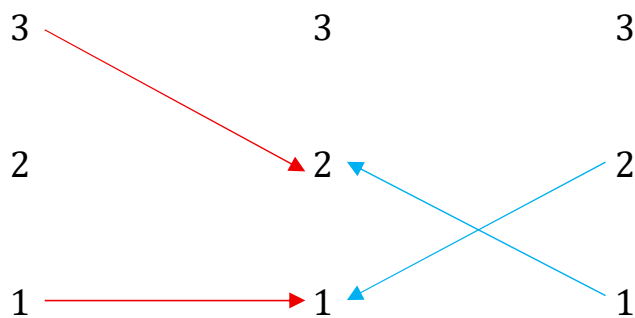
$ZKI = (3.1, 2.1, 1.2)$

Methode 1

$(3.1, 2.1, 1.2)' = ((3.2, 1.1), (2.1, 1.2))$

$((3.2, 1.1), (2.1, 1.2))' = ((3.1, 2.1), (2.1, 1.2))$

$((3.1, 2.1), (2.1, 1.2))' = ((3.2, 1.1), (2.1, 1.2)) \#$

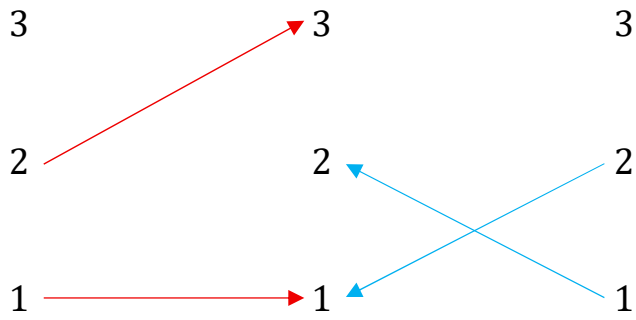


Methode 2

$(3.1, 2.1, 1.2)' = ((1.1, 2.3), (2.1, 1.2))$

$((1.1, 2.3), (2.1, 1.2))' = ((3.1, 2.1), (2.1, 1.2))$

$((3.1, 2.1), (2.1, 1.2))' = ((1.1, 2.3), (2.1, 1.2)) \#$



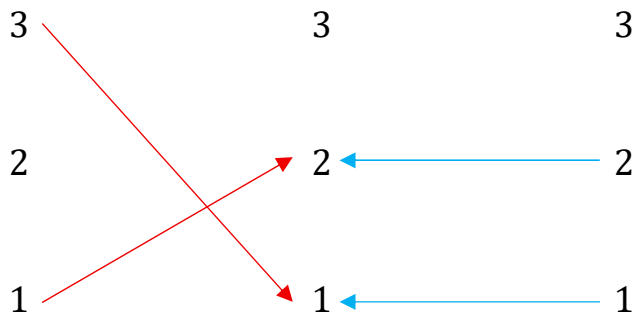
Methode 3

$$(3.1, 2.1, 1.2)' = ((1.2, 3.1), (1.1, 2.2))$$

$$((1.2, 3.1), (1.1, 2.2))' = ((2.3, 1.1), (1.2, 1.2))$$

$$((2.3, 1.1), (1.2, 1.2))' = ((3.1, 2.1), (2.1, 1.2))$$

$$((3.1, 2.1), (2.1, 1.2))' = ((1.2, 3.1), (1.1, 2.2)) \#$$



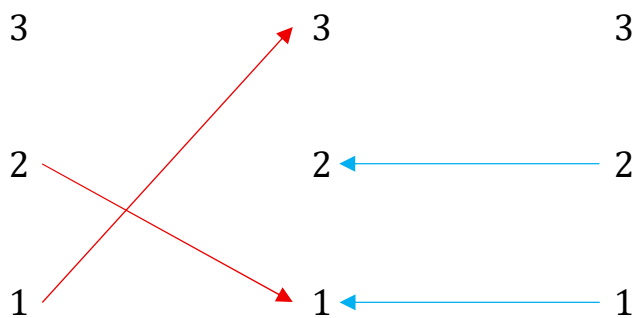
Methode 4

$$(3.1, 2.1, 1.2)' = ((1.3, 2.1), (2.2, 1.1))$$

$$((1.3, 2.1), (2.2, 1.1))' = ((1.1, 2.3), (1.2, 1.2))$$

$$((1.1, 2.3), (1.2, 1.2))' = ((3.1, 2.1), (2.1, 1.2))$$

$$((3.1, 2.1), (2.1, 1.2))' = ((1.3, 2.1), (2.2, 1.1)) \#$$



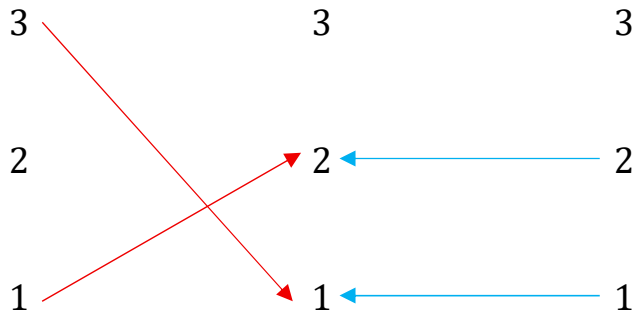
Methode 5

$$(3.1, 2.1, 1.2)' = ((3.1, 1.2), (2.2, 1.1))$$

$$((3.1, 1.2), (2.2, 1.1))' = ((3.2, 1.1), (2.1, 2.1))$$

$$((3.2, 1.1), (2.1, 2.1))' = ((3.1, 2.1), (2.1, 1.2))$$

$$((3.1, 2.1), (2.1, 1.2))' = ((3.1, 1.2), (2.2, 1.1)) \#$$



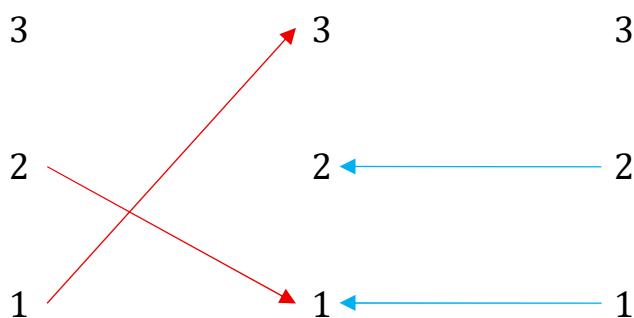
Method 6

$$(3.1, 2.1, 1.2)' = ((2.1, 1.3), (1.1, 2.2))$$

$$((2.1, 1.3), (1.1, 2.2))' = ((1.1, 3.2), (2.1, 2.1))$$

$$((1.1, 3.2), (2.1, 2.1))' = ((3.1, 2.1), (2.1, 1.2))$$

$$((3.1, 2.1), (2.1, 1.2))' = ((2.1, 1.3), (1.1, 2.2)) \#$$



Method 7

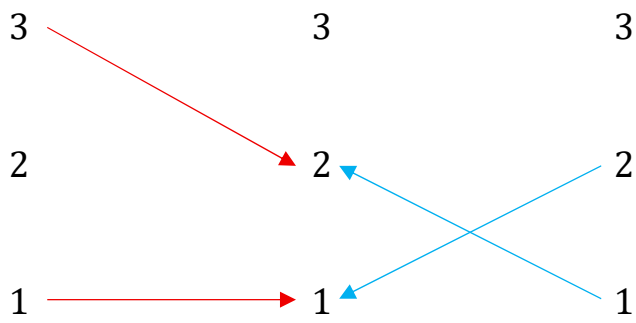
$$(3.1, 2.1, 1.2)' = ((1.1, 3.2), (1.2, 2.1))$$

$$((1.1, 3.2), (1.2, 2.1))' = ((1.2, 1.3), (2.1, 1.2))$$

$$((1.2, 1.3), (2.1, 1.2))' = ((2.3, 1.1), (1.2, 2.1))$$

$$((2.3, 1.1), (1.2, 2.1))' = ((3.1, 2.1), (2.1, 1.2))$$

$$((3.1, 2.1), (2.1, 1.2))' = ((1.1, 3.2), (1.2, 2.1)) \#$$



Methode 8

$(a.b), (c.d) = 8. (c.a), (d.b)$

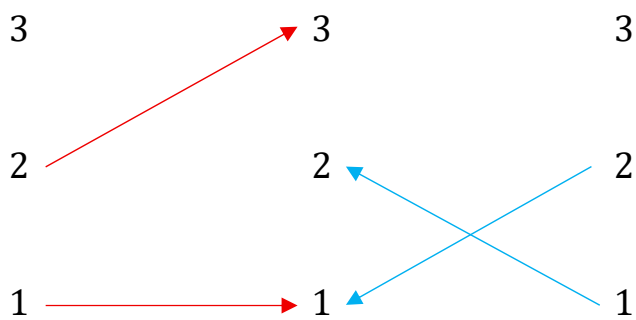
$(3.1, 2.1, 1.2)' = ((2.3, 1.1), (1.2, 2.1))$

$((2.3, 1.1), (1.2, 2.1))' = ((1.2, 1.3), (2.1, 1.2))$

$((1.2, 1.3), (2.1, 1.2))' = ((1.1, 3.2), (1.2, 2.1))$

$((1.1, 3.2), (1.2, 2.1))' = ((3.1, 2.1), (2.1, 1.2))$

$((3.1, 2.1), (2.1, 1.2))' = ((2.3, 1.1), (1.2, 2.1)) \#$



Es gilt:

$M1 = M7$

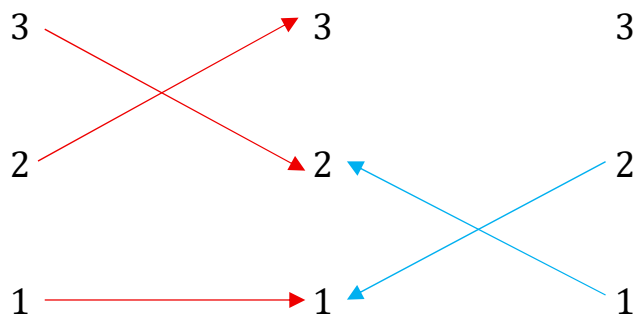
$M2 = M8$

$M3 = M5$

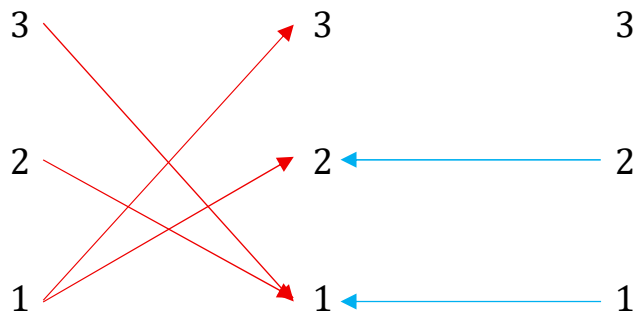
$M4 = M6$

3. Vereinigungsgraphen

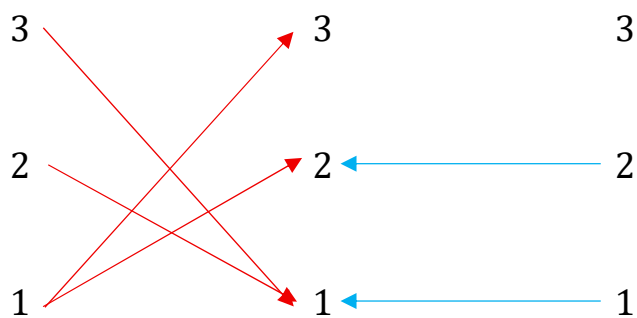
$\cup(M1, M2)$



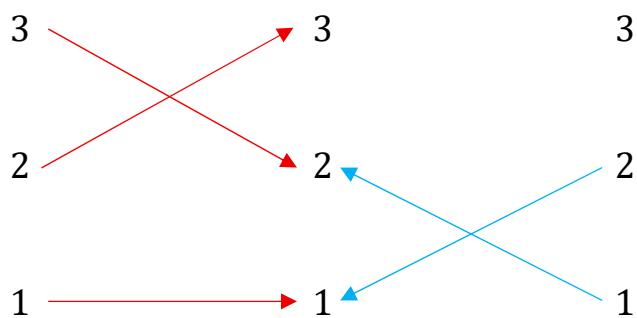
$\cup(M3, M4)$



$\cup(M5, M6)$



$\cup(M7, M8)$



Es gilt somit:

$$\cup(M1, M2) = \cup(M7, M8)$$

$$\cup(M3, M4) = \cup(M5, M6).$$

Die Vereinigungsgraphen jedes der vier Paare von bifunktoriellen Ableitungen lassen sich also auf nur zwei Paare zurückführen.

Literatur

Toth, Alfred, Semiotische Differentiation. In: Electronic Journal for Mathematical Semiotics, 2025a

Toth, Alfred, Semiotische Differentiation II. In: Electronic Journal for Mathematical Semiotics, 2025b

28.9.2025